

## Lactation curves of Holstein x Gyr dual-purpose cows under humid tropical conditions

### Curvas de lactación de vacas de doble propósito Holstein x Gyr bajo condiciones de trópico húmedo

Jorge Alonso Peralta-Torres<sup>1</sup>, Yuliana Izquierdo-Camacho<sup>1</sup>, Nadia Florencia Ojeda-Robertos<sup>1</sup>, Víctor Hugo Severino-Lendechy<sup>2</sup>, Jesús Enrique Ek-Mex<sup>3</sup>, José Candelario Segura-Correa<sup>4,\*</sup>

#### ABSTRACT

The aim of this study was to identify the foremost model that depict the lactation curve of dual-purpose crossbred cows under a humid tropical environment. Six models were compared to describe the lactation curves of three breed groups using 1231 milk records of 160 cows. The breed groups were 0-25%, F1 (50%) and 62.5-75% Holstein x Gyr crosses. Parameters of the models and curves were estimated using non-linear procedures. The best model was determined by the Akaike information criterion. Wood, Sikka and Wilmink models provided a good fit to the lactation curves for the breed groups; however, the Wood model was applied to depict the lactation curves, the day at which lactation peak was reached and milk yield at the peak. The aspect of the curves differed according to the breed group. The low graded Holstein cows had typical standard curves, and the

<sup>1</sup> División Académica de Ciencias Agropecuarias, Universidad Juárez Autónoma de Tabasco, Tabasco, México

<sup>2</sup> Centro de Estudios Etnoagropecuarios, Universidad Autónoma de Chiapas, Chiapas, México

<sup>3</sup> Centro de Bachillerato Tecnológico Agropecuario 283, Unidad de Educación Media Superior Tecnológica Agropecuaria y Ciencias del Mar, Yucatán, México

<sup>4</sup> Facultad de Medicina Veterinaria y Zootecnia, Universidad Autónoma de Yucatán, Mérida, Yucatán, México

\* E-mail: jose.segura@correo.uady.mx

Received: March 14, 2022

Accepted for publication: November 1, 2022

Published: December 22, 2022

©Los autores. Este artículo es publicado por la Rev Inv Vet Perú de la Facultad de Medicina Veterinaria, Universidad Nacional Mayor de San Marcos. Este es un artículo de acceso abierto, distribuido bajo los términos de la licencia Creative Commons Atribución 4.0 Internacional (CC BY 4.0) [<https://creativecommons.org/licenses/by/4.0/deed.es>] que permite el uso, distribución y reproducción en cualquier medio, siempre que la obra original sea debidamente citada de su fuente original

F1 and high graded cows had no lactation curve peak. Milk yield at start of lactation increased as the Holstein blood increased. The rate of milk per day was close to zero (0.0813 for 0-25% Holstein cows; 0.0247 for F1 and 0.0023 kg/day for 62.5-75% Holstein cows). The aspect of the lactation curve varied depending on the non-linear model and the grade of Holstein. The shapes of the lactation curves vary according to the breed group from normal to without peak milk yield.

**Key words:** breed group, lactation peak, Sikka, Wilmink, Wood model

## RESUMEN

El objetivo del estudio fue identificar el principal modelo que represente la curva de lactancia de vacas cruzadas de doble propósito en un ambiente tropical húmedo. Se compararon seis modelos para describir las curvas de lactancia de tres grupos raciales utilizando 1231 registros de leche de 160 vacas. Los grupos raciales fueron 0-25%, F1 (50%) y 62.5-75% cruces Holstein x Gyr. Los parámetros de los modelos y las curvas se estimaron mediante procedimientos no lineales. El mejor modelo fue determinado por el criterio de información de Akaike. Los modelos Wood, Sikka y Wilmink proporcionaron un buen ajuste de las curvas de lactancia; sin embargo, se aplicó el modelo de Wood para representar las curvas de lactancia, el día en que se alcanzó el pico de lactancia y la producción de leche en el pico. El aspecto de las curvas difirió según el grupo racial. Las vacas de bajo grado Holstein tuvieron curvas estándar típicas, pero las vacas F1 y de grado alto no presentaron el pico de la curva de lactancia. La producción de leche al inicio de la lactancia aumentó a medida que aumentaba la sangre Holstein. La tasa de leche por día fue cercana a cero (0.0813 para 0-25 %, 0.0247 para F1 y 0.0023 kg/día para 62.5-75 % de vacas Holstein). El aspecto de la curva de lactancia varió según el modelo no lineal y el grado de Holstein. Las formas de las curvas de lactancia variaron según el grupo racial, desde normal hasta no presentar pico de lactación.

**Palabras clave:** grupo racial, pico de lactancia, Sikka, Wilmink, modelo de Wood

## INTRODUCTION

Dual purpose production system is the most common way to produce milk and meat from cattle in the tropics of the world and in those of Mexico. Milk is important to feed the calf and for human consumption; therefore, it is important to know the potential milk production of dual-purpose cows to improve total milk production per lactation. Dairy cows' lactation curve in specialized systems show an increase from calving up to a peak milk yield between weeks 4 and 8 of lactation, pursue by a reduction in milk until being dried-off (Macciotta *et al.*, 2005). In addition, it is known that environmental factors

affect the milk production of cows under temperate conditions, such as breed, season of calving and parity number (Kunaka and Makuza, 2005; Karadas and Birinci, 2019) and in consequence the shape of the lactation curve changes (Guler and Yanar, 2009). However, studies about lactation curves of crossbred *Bos taurus* x *Bos indicus* cows under the humid tropical conditions of Mexico are scarce. Some studies in crossbred cattle in the tropics suggest the effect of breed group, season and parity number in the form of the curve of lactation (Osorio-Arce and Segura Correa, 2005). However, much of those studies have been carried out under subhumid-tropical conditions. Differences exist between the subhumid and humid tropics

of Mexico, due to amount of rain, its effect on pasture availability and level of stress caused by environmental conditions and disease.

Many equations have been tested to describe the lactation curves, the most widely applied being those of the non-linear type. Some of the most used models are Brody, Dijkstra, Wilmink and Wood (Val-Arreola *et al.*, 2004; Kawata, 2011; Khan *et al.*, 2012). The choose of the correct statistical model is important to make management decisions and to predict milk production per cow and during its lifetime. It is also important to know the peak of production, persistency of milk, and age and weight at maturity. Therefore, it is worth to depict the shape of the lactation curve of dual-purpose cows under the Mexican tropical conditions. The aim of this study was to estimate the parameters and to describe the lactation curve of multiparous dual-purpose cows (Holstein x Gyr) under the humid tropical conditions of the southeast of Mexico.

## MATERIALS AND METHODS

### Location of the Study

The production unit was located at the north of Chiapas Mexico. The area has a humid-tropical environment, high mean temperature (26.5 °C), and high annual rainfall (about 3250 mm), most of which falls during June and September (INEGI, 2021). The lactation records used in this study included 1231 test-day milk yield data obtained from 160 dual-purpose Holstein x Gyr cows collected during November 2017 to February 2019.

### Management and Breed Groups

Cows in the studied herd belongs to three breed groups: 0-25%, F1 (50%) and 62.5-75% Holstein x Gyr. They grazed on star grass (*Cynodon plectostachyus*), milked once a day, and they were given 2 kg of a

Table 1. Models used to describe the lactation curve of three breed groups of Holstein x Gyr cows kept under humid tropical conditions

Function name	Lactation curve model
Polinomial	$y_t = b_0 + b_1 t + b_2 t^2 + b_3 t^3 + b_4 t^4$
Brody	$y_t = b_0 \exp(-b_1 t) + b_0 \exp(-b_2 t)$
Sikka	$y_t = b_0 \exp(b_1 t - b_2 t^2)$
Dijkstra	$y_t = b_0 * \exp(b_1(1 - e^{-b_2 t}) / c - b_3 t)$
Wilmink	$y_t = b_0 + b_1 \exp(-0.06 t) + b_2 t$
Wood	$y_t = b_0 t^{b_1} \exp(-b_2 t)$

$y_t$  = milk production per cow the day  $t$  (L/day);  $b_0$ ,  $b_1$ ,  $b_2$ ,  $b_3$ ,  $b_4$  coefficients that describe the shape of the lactation curve

commercial feed concentrate (16% crude protein and 2.3 Mcal EM/kg). Calves were submitted to a restrict feeding, had access to one teat during the first month of lactation and thereafter they only suckled the residual milk. Milk yield was weighed at approximately 14 day-intervals and included only the extracted milk, excluding that consumed by the calf. Cows were vaccinated against common diseases of the region.

### Lactation Curve Models

Six functions were used to model the lactation curve and to estimate lactation curve parameters for cows with 3 to 6 parities. The curve fitting was carried out applying the algorithm of Gauss-Newton in the NLIN procedure (SAS, 2012). The lactation curve models used to describe milk yield with time are shown in Table 1. In normal curves,  $Y_t$  is the milk production at day  $t$  of measure;  $b_0$  is the parameter estimated related with milk yield at the start of lactation,  $b_1$  is a parameter correlated with the ascending phase of the curve before peak yield, and  $b_2$  is the parameter estimated correlated with the declining phase after the peak yield is reached.

The formulas to estimate the number of days up to the peak milk yield (DIMP) and the yield of milk (kg) at the peak of the lactation curve for the Wood model were estimated as:  $b_1/b_2$  and  $b_0(b_1/b_2)^{b_1} \exp^{-b_1}$ , respectively.

**Ethical Standards**

The manuscript does not contain clinical studies or patient data. Data were obtained from the record books where milk information was kept.

**Statistical Analysis**

A total of 1231 milk records from 160 lactations from same number of cows ranging from 105 to 270 days in length were used. Milk was registered for each cow approximately every two weeks. Lactations starting after 28 days of calving were not included in the study (n=16).

The milk data were captured into Microsoft Excel data sheets and then imported into SAS (2012) for posterior data

debugging and fitting in the best lactation curve. All non-linear models were fitted using NLIN procedure (SAS, 2012).

The goodness-of-fit of the best model was determined using the Akaike Information Criterion (AIC). However, the root of the mean squares of the prediction error (RMSPE) and coefficient of determination ( $R^2$ ) were also calculated. Smaller values of AIC and RMSPE and higher of  $R^2$  indicate a better fit when two models are compared. AIC were calculated from the results provided by NLIN as suggested by Motulsky and Christopoulos (2003):  $AIC = n * (\ln(SSE/n)) + 2k + 2k * (k+1) / (n-k-1)$ , where n is the number of records, ln is the logarithm base 2.718, SSE is the sum of squares of the residual provide by the NLIN procedure, and k means the number of parameters involve in the non-linear model. The probability of choosing between two models was calculated as  $p = \exp(-|AIC \text{ difference}|/2) / (1 + \exp(-|AIC \text{ difference}|/2))$ ; where a  $p < 0.05$  indicates difference between the two models being compared (Motulsky and Christopoulos, 2003).

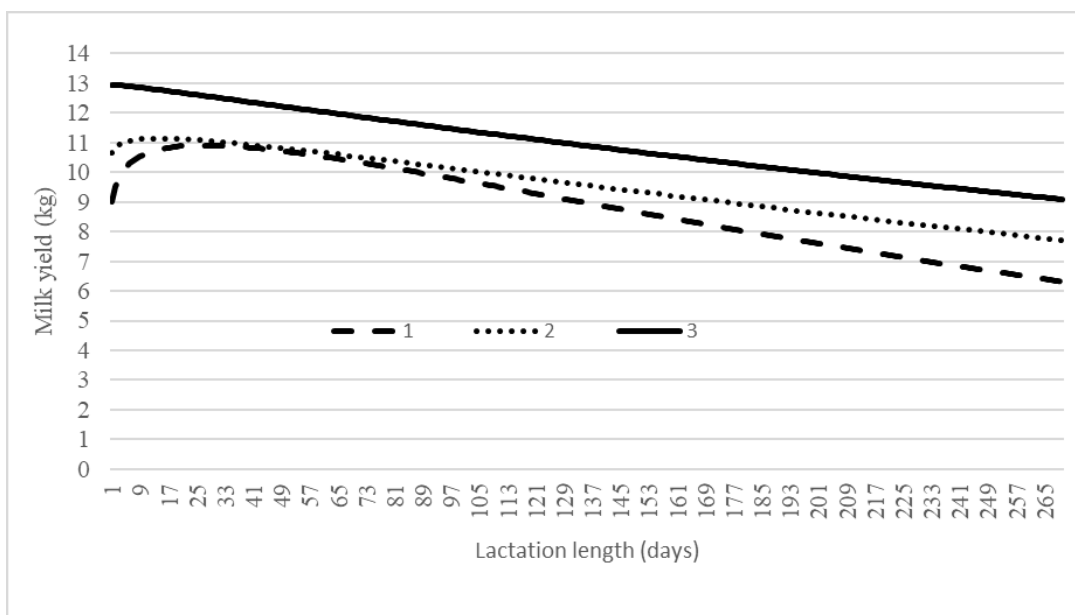


Figure 1. Wood model predicted lactation curves for 0-25% (1), 50% (2) and 62.5-75% (3) Holstein x Gyr cows in the humid tropics of Mexico

## RESULTS

The RMSPE, AIC and  $R^2$  for each model are shown in Table 2. There were no differences among Wood, Wilmink and Sikka models being better than the Polynomial model. The Brody equation has problem to converge for the high graded Holstein x Gyr group. In this group, the Brody model converge, but a problem with the model was advised by SAS. Dijkstra model did not converge for any of the three breed groups.

The shape of the lactation curves for the three breed groups based on the Wood model is shown in Figure 1. Differences in the appearance of the lactation curve between breed groups were observed, especially in the number of days at the peak, the slope, and the flatness of the curves. The

days at peak milk yield for the 0-25, 50 and 62.5-75% Holstein graded cows were 26.9, 14.4 and 1.7 days, respectively.

The parameter values of the lactation curves are shown in Table 3. In the Wood model the  $b_1$  and  $b_2$  coefficients were positive and close to zero for the F1 and 62.5-75% Holstein x Gyr cows. The  $b_1$  value of the 0-25% Holstein x Gyr cows was also low 0.0813, but 3.29 and 35.35 times greater than those for the F1 and highly graded cows which affected the shape of the lactation curve.

## DISCUSSION

### Model Fit

There were no differences among Wood, Wilmink and Sikka models based on-

Table 3. Parameter estimates of models used to describe the lactation curve of Holstein x Gyr cows

Function	$b_0$	$b_1$	$b_2$	$b_3$	$b_4$
0-25% Holstein (n=409)					
Polynomial	10.50±0.787	0.0258±0.0392	-0.0005±0.00060	2.077E-6	-2.54E-9
Brody	-12.02±0.326	0.2106±0.0453	0.00225±0.00022		
Dijkstra	-----	-----	-----	-----	-----
Sikka	11.35±0.430	-0.0013±0.0008	3.205E-6±3.148E-6		
Wilmink	11.86±0.326	-2.1991±1.234	-0.0211±0.00222		
Wood	9.056±1.176	0.0813±0.0403	0.00302±0.00052		
50% Holstein (n=769)					
Polynomial	11.92±0.551	-0.0480±0.0280	0.00055±0.000421	-3.02E-6	5.736E-9
Brody	-11.63±0.215	0.4320±0.01385	0.00148±0.000139		
Dijkstra	-----	-----	-----	-----	-----
Sikka	11.23±0.302	-0.00073±0.00052	2.88E-6±2.054E-6		
Wilmink	11.51±0.247	-0.2628±0.8624	-0.0143±0.00159		
Wood	10.70±0.902	0.0247±0.0263	0.00172±0.000332		
62.5-75% Holstein (n=208)					
Polynomial	14.84±1.489	-0.126±0.0729	0.00165±0.00107	-8.63E-6	1.469E-8
Brody	-----	-----	-----	-----	-----
Dijkstra	-----	-----	-----	-----	-----
Sikka	12.54±0.707	-0.0004±0.0011	3.809E-6±4.276E-6		
Wilmink	12.77±0.581	1.154±2.471	-0.0139±0.00370		
Wood	12.95±2.69	0.0023±0.0064	0.00136±0.00075		

$b_0, b_1, b_2, b_3, b_4$  coefficients that define the shape of the lactation curve.

the comparison of AIC and the formula to determine the best of two models. Considering the AIC, the Wood model was used to depict the lactation curve, the aspect of the lactation curve and model parameter estimates for the three breed groups. In addition, the Wood model is commonly used to depict the lactation curves of dairy cattle (Val-Arreola *et al.*, 2004; Gradiz *et al.*, 2009; Macciotta *et al.*, 2011).

The difference of fit of the models between breed groups may be due to different genetic potential for milk production of the breed groups. Pure Holstein cows are recognized because of its high milk yield capability, and the pure Zebu cows for their adaptation to the tropical climate, and resistance to parasites and diseases. Some authors from tropical countries suggest that the F1 cross of dairy cattle from temperate climate and those from tropical breeds produce more milk per day than pure breed cows under tropical environments (Syrstad, 1989; Madalena *et al.*, 1990). Peralta-Torres *et al.* (2022) using the same source of data of this study, showed short lactation length and total milk yield per lactation for 0-25% Holstein x Gyr, compared to F1 and 62.5-75% Holstein x Gyr cows, but without significant differences between the last two breed groups.

### Lactation Curve Shape

The lactation curve of the 0-25% Holstein x Gyr cows was similar to the shape of typical lactation curves notified for Holstein cows under temperate climates (Tozer and Huffaker, 1999; Moraes-Concalves *et al.*, 2002), showing a sharp increase followed by a gradual decline after the peak, until cows are dried-off. Typical shape curves were also observed by other authors (Osorio-Arce and Segura-Correa, 2005) under humid tropical conditions in Tabasco, Mexico, for  $\frac{3}{4}$  Holstein  $\frac{1}{4}$  Zebu and F2 generation of  $\frac{1}{2}$  Holstein  $\frac{1}{2}$  Sahiwal cows. On the other hand, the curves for F1 and 62.5-75% Holstein x Gyr cows corresponded to those reported for dual-purpose cattle in the tropics, which showed

to be negative linear with a slight or no peak of milk production. Atypical curves are distinguished by the lack of a lactation peak (Boujenane and Hilal, 2012; Jeretina *et al.*, 2013; Chegini *et al.*, 2015) and are partially due to variations in the amount and quality of feeds, as well as to physiological and health complications associated with hard environmental conditions. Here, it could be associated with pasture quality and quantity across the year. However, it is worth to mention that cows in this study were given 2 kg of a feed supplement (16% CP and 2.3 Mcal ME/kg) during the critical months of the year. Furthermore, the variation in the aspect of curve is also attributed to the effect of season due to better quality of pasture in spring (Macciotta *et al.*, 2011).

### Lactation Curve Parameters

The differences in the shape of the lactation curve between groups can be attributed, among other reasons, to differences in the model parameter estimates for each breed group (Table 3). The shape of the curve for 0-25% Holstein cows were more similar to the normal lactation curve, but with lower milk yield at the beginning of lactation period than the other groups. F1 and 62.5-75% Holstein cows had atypical lactation curve shapes (Figure 1).

The milk yield at the start of the lactation period (intercept) here obtained (Table 3) was greater than those estimated for  $\frac{3}{4}$  Holstein  $\frac{1}{4}$  Zebu (7.49 kg) and the F2 generation of  $\frac{1}{2}$  Holstein  $\frac{1}{2}$  Sahiwal cows (6.70 kg) in the Mexican humid tropics (Osorio-Arce and Segura-Correa, 2005). Moreover, it was greater than the 4.67 kg reported for Holstein x Brahman, Holstein x Brown Swiss and Brown Swiss x Brahman crossbred cows in Honduras (Gradiz *et al.*, 2009), but agree to values reported by Madalena *et al.* (1979) for F1 Holstein x Gyr (12.81 kg),  $\frac{3}{4}$  Holstein x  $\frac{1}{4}$  Gyr (11.36 kg) and pure Holstein (10.91 kg). The higher daily milk yields in this study were due to the use of Gyr cows in the cross with Holstein.

The form of the lactation curve is depicted by the parameters of the model used. In the Wood model, positive values for  $b_1$  and  $b_2$  give a normal curve with a milk peak. A curve with negative  $b_1$  and  $b_2$  parameter estimates provide a negative linear curve as that for 62.5 to 75% Holstein cows (Figure 1). As an example, Khan *et al.* (2012) using the Nelder model found an increase in the rate of milk ( $b_1$ ) up to the peak of the lactation curve various breeds and crosses. The positive values of  $b_1$  and  $b_2$  for the 0-25% breed group (0.081 and 0.003 kg/day, respectively) in the study were lower than those reported in crossbred female (Gradiz *et al.*, 2009), and in Holstein x Zebu (0.178 and 0.366 kg/day) and Holstein x Sahiwal (0.196 and 0.364 kg/day) under tropical humid conditions of Tabasco, Mexico (Osorio-Arce and Segura-Correa, 2005).

#### Days at Peak and Milk Yield at Peak

Only the 0-25% Holstein x Gyr cows showed a lactation peak, and this occurred at day 26.92 with the highest milk yield of 10.91 kg, being lower than the means notified by Tekerli *et al.* (2000) and Chegini *et al.* (2015) in Holstein cattle. However, those values were close to the ones reported in Mexico (5) for Holstein x Zebu and Holstein x Sahiwal cows (11.89 and 11.01 kg, respectively).

#### CONCLUSIONS

- Wood, Wilmink and Sikka models described the lactation curves of the three breed groups (0-25, 50 and 62.5-75% Holstein x Gyr) and were similar in the criteria of fit.
- Breed groups showed differences in the shape of the lactation curves

#### Acknowledgements

The authors thank the lawyer Ever Velasco Bernal owner of the Ranch «La Esperanza» for providing the milk data for this study.

#### REFERENCES

1. **Boujenane I, Hilal B. 2012.** Genetic and non genetic effects for lactation curve traits in Holstein-Friesian cows. *Arch Anim Breed* 55: 450–457. doi: 10.5194/aab-55-450-2012
2. **Chegini A, Hossein-Zadeh NG, Hosseini-Moghadam H. 2015.** Effect of calf sex on some productive, reproductive and health traits in Holstein cows. *Spanish J Agric Res* 13: e0605. doi: 10.5424/sjar/2015132-6320
3. **Gradiz L, Alvarado L, Kahi AK, Hirooka H. 2009.** Fit of Wood's function to daily milk records and estimation of environmental and additive and non-additive genetic effects on lactation curve and lactation parameters of crossbred dual purpose cattle. *Livest Sci* 124: 321-329. doi: 10.1016/j.livsci-2009.02.016
4. **Guler O, Yanar M. 2009.** Factors influencing the shape of lactation curve and persistency of Holstein Friesian cows in high altitude of Eastern Turkey *J Appl Anim Res* 35: 39-44. doi: 10.1080/09712119.2009.9706981
5. **[INEGI] Instituto Nacional de Estadística y Geografía. 2021.** Banco de indicadores. Mexico.[Internet]. Disponible en: <https://www.inegi.org.mx/app/indicadores/?ag=07048>
6. **Jeretina J, Babink D, Skorjance D. 2013.** Modelling lactation curve standards for test day milk yield in Holstein, Brown Swiss and Simmental cows. *J Anim Plant Sci* 233: 754-62.
7. **Karadas K, Birinci A. 2019.** Determination of factors affecting dairy cattle: a case study of Ardahan province using data mining algorithms. *Rev Bras Zootec* 48: e20170263. doi: 10.1590/rbz4820170263
8. **Kawata Y. 2011.** Lactation curves of dairy animals: an interim literature review. *Res Bull Obihiro Univ* 32: 71-91

9. **Khan MKI, Blair HT, Lopez-Villalobos N. 2012.** Lactation curves of different cattle breeds under cooperative dairying conditions in Bangladesh. *J Applied Anim Res* 40: 179-185. doi: 10.1080/09712119.-2011.645039
10. **Kunaka K, Makuza SM. 2005.** Environmental factors affecting milk production in the Holstein-Friesian population of Zimbabwe. *Pakistan J Biol Sci* 8: 989-994. doi: 10.3923/pjbs.2005.-989.994
11. **Macciotta NPP, Vicario D, Cappio-Borlino A. 2005.** Detection of different shapes of lactation curve for milk yield in dairy cattle by empirical mathematical models. *J Dairy Sci* 88: 1178-1191. doi: 10.3168/jds.S0022-0302(05)72784-3
12. **Macciotta NPP, Dimauro C, Rassu S. PG, Steri R, Pulina G. 2011.** The mathematical description of lactation curves in dairy cattle. *Italian J Anim Sci* 10: e51. doi: 10.4081/ijas.2011.e51
13. **Madalena FE, Martínez ML, Freitas AF. 1979.** Lactation curves of Holstein-Friesian and Holstein-Friesian x Gir cows. *Anim Prod* 29: 101-107. doi: 10.1017/S0003356100012198
14. **Madalena FE, Teodoro RL, Lemos AM, Monteiro JBN, Barbosa RT. 1990.** Evaluation of strategies for crossbreeding of dairy cattle in Brazil. *J Dairy Sci* 73: 1887-1901. doi: 10.3168/jds.S0022-0302(90)78869-8
15. **Moraes-Concalves T, Gomes de Oliveira AI, Fonseca de Freitas RT, García Pereira I. 2002.** Curvas de lactacao em rebanhos da raca Holandesa no estado de Minas Gerais. Escolha do modelo de melhor ajuste. *R Bras Zootec* 31: 1689-1694. doi: 10.1590/S1516-35982002000700011
16. **Motulsky HJ, Christopoulos A. 2003.** Fitting models to biological data using linear and nonlinear regression. A practical guide to curve fitting. San Diego, USA: GraphPad Software. 351 p.
17. **Osorio-Arce MM, Segura-Correa JC. 2005.** Factores que afectan la curva de lactancia de vacas Bos taurus x Bos indicus en un sistema de doble propósito en el trópico húmedo de Tabasco, México. *Téc Pecu Méx* 43: 127-137.
18. **Peralta-Torres J, Izquierdo-Camacho Y, Severino-Lendechy V, Segura-Correa J. 2022.** Producción de leche de vacas Holstein x Gyr en un sistema de doble propósito en el trópico. *Rev MVZ Córdoba* 27: e2359. doi: 10.21897/rmvz.2359
19. **SAS. 2012.** Institute. User is Guide. Version 9.4 ed. Cary, (NC) USA: SAS Institute Inc.
20. **Syrstad O. 1989.** Dairy cattle crossbreeding in the tropics: performance of secondary crossbred populations. *Livest Prod Sci* 23: 97-106. doi: 10.1016/0301-6226(89)90008-0
21. **Tekerli M, Akinci Z, Dogan I, Akcan A. 2000.** Factors affecting the shape of lactation curves of Holstein cows from the Balikesir province of Turkey. *J Dairy Sci* 83: 1381-1386. doi: 10.3168/jds.S0022-0302(00)75006-5
22. **Tozer PR, Huffaker RG. 1999.** Mathematical equations to describe lactation curves for Holstein-Friesian cows in New South Wales. *Aust J Agric Res* 50: 431-440. doi: 10.1071/A98064
23. **Val-Arreola D, Kebreab E, Dijkstra J, France J. 2004.** Study of the lactation curve in dairy cattle on farms in Central Mexico. *J Dairy Sci* 87: 3789-3799. doi: 10.3168/jds.S0022-0302(04)73518-3